



Class: XI  
Date: 28.05.2024

Sub: MATHEMATICS (041)

Max Marks: 30  
Time: 1 hr

**General Instructions:**

1. This question paper is divided into 4 sections- A, B, C and D.
2. Section A comprises of 7 questions of 1 mark each.
3. Section B comprises of 3 questions of 2 marks each.
4. Section C comprises of 3 questions of 3 marks each.
5. Section D comprises of 2 case study-based questions
6. Internal choice has been provided for certain questions

**Section – A**

- 1 The number of non-empty subsets of a set, containing  $n$  elements, is  
(a)  $n$  (b)  $n^2$  (c)  $2^n$  (d)  $2^n - 1$
  - 2 Which of the following statement is false?  
(a)  $A - B = A \cap B'$  (b)  $A - B = A - (A \cap B)$   
(c)  $A - B = A - B'$  (d)  $A - B = (A \cup B) - B$
  - 3 Let  $R$  be a relation on  $N$  defined by  $R = \{(x, y) : x + 2y = 8, x, y \in N\}$ . Then domain of  $R$  is  
(a)  $\{2, 4, 8\}$  (b)  $\{2, 4, 6, 8\}$  (c)  $\{2, 4, 6\}$  (d)  $\{1, 2, 3, 4\}$
  - 4 If  $f(x) = x^3 - \frac{1}{x^3}$ , then  $f(x) + f\left(\frac{1}{x}\right)$  is equal to  
(a)  $2x^3$  (b)  $\frac{2}{x^3}$  (c) 0 (d) 1
  - 5 If  $(x + 3, 5) = (6, 2x + y)$  then  $x, y$  is equals to  
(a) 3, -1 (b) 3, 0 (c) 0, -1 (d) None of these
  - 6 Which of the following is not correct?  
(a)  $\sin \theta = -\frac{1}{5}$  (b)  $\cos \theta = 1$  (c)  $\sec \theta = \frac{1}{2}$  (d)  $\tan \theta = 20$
  - 7 **Assertion (A):**  $\sin(-270)^\circ = 1$ .  
**Reason (R):**  $\sin(180^\circ + \theta) = \sin \theta$   
(A) Both A and R are true and R is the correct explanation of A  
(B) Both A and R are true but R is NOT the correct explanation of A  
(C) A is true but R is false  
(D) A is false and R is True
- (a)  $2\sqrt{3}$  (b) 4 (c) 1 (d) 0

## Section – B

- 8 If  $\sin x = -\frac{5}{13}$ ,  $x$  lies in III quadrant, find the values of  $\sin \frac{x}{2}$ ,  $\cos \frac{x}{2}$  and  $\tan \frac{x}{2}$ .
- 9 Let  $A = \{1, 2, 3, 4, 5, 6\}$ . Let  $R$  be a relation on  $A$  defined by  $R = \{(a, b) : b \text{ is exactly divisible by } a; a, b \in A\}$ , then  
 (i) Write  $R$  in roster form.                      (ii) Find the domain of  $R$ .                      (iii) Find the range of  $R$ .
- 10 If  $A = \{x : x \in R, x \text{ is the root of the equation } x^3 - x = 0\}$ , and  
 $B = \{x : x \in R, x \text{ is the root of } x^3 + 2x^2 - x - 2 = 0\}$   
 Then find the values of (i)  $A \cup B$  (ii)  $A \cap B$

## Section – C

- 11 Draw appropriate Venn diagrams for each of the following:  
 (i)  $A \cup B$                       (ii)  $A \cap B$                       (iii)  $(A - B) \cup (B - A)$
- 12 Prove that  $\sqrt{2 + \sqrt{2 + 2\cos 4x}} = 2\cos x$
- 13 Prove that if  $\tan A = x \tan B$ , then  $\frac{\sin(A-B)}{\sin(A+B)} = \frac{x-1}{x+1}$

## Section – D

- 14 Students of Indian Public School was conducting a quiz. The questions for round was as follows. The participants are required to finish the task in five minutes  
 (i) If  $A = \{-1, 1\}$ , then the find the number of elements in  $A \times A \times A$  (2m)  
 (ii) Find the domain and range of the function  
 $f(x) = \sqrt{25 - x^2}$  (2m)



- 15 Salman and Amir are solving math question from chapter sets of class XI.  
 Given  $U = \{x : x \leq 25, x \in N\}$ ,  
 $A = \{x : x \leq 15, x \in N\}$  and  
 $B = \{x : 10 < x \leq 25, x \in N\}$ .  
 In few questions they are not confident about their answer. Find the answer for the following questions and help Salman and Amir to verify their answers.
- (i) Find  $B - A$  (1m)  
 (ii) Find  $A \cup B$  (1m)  
 (iii) Find  $(A - B)'$  (2m)  
 - OR -  
 Find  $A' \cap B'$





# INDIAN SCHOOL AL WADI AL KABIR

## Unit Test – Model Paper (2024 - 2025)

### Answer Key

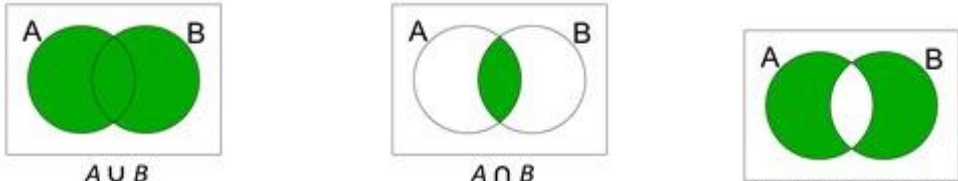
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1	(d) $2^n - 1$
2	(c) $A - B = A - B'$
3	(c) $\{2, 4, 6\}$
4	(c) 0
5	(a) 3, -1
6	(c) $\sec \theta = \frac{1}{2}$
7	(C) A is true but R is false
8	$\cos x = -\frac{12}{13}$ $\cos x = 2\cos^2 \frac{x}{2} - 1$ $-\frac{12}{13} = 2\cos^2 \frac{x}{2} - 1$ $\Rightarrow \cos^2 \frac{x}{2} = \frac{1}{26}$ $\Rightarrow \cos \frac{x}{2} = -\frac{1}{\sqrt{26}}$ Similarly $\sin \frac{x}{2} = \frac{5}{\sqrt{26}}$ And $\tan \frac{x}{2} = -5$
9	(i) $R = \{(1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (1, 6), (2, 2), (2, 4), (2, 6), (3, 3), (3, 6), (4, 4), (5, 5), (6, 6)\}$ (ii) Domain = $\{1, 2, 3, 4, 5, 6\}$ (iii) Range = $\{1, 2, 3, 4, 5, 6\}$
10	$A = \{0, -1, 1\}$ and $B = \{-2, -1, 1\}$ $A \cup B = \{0, -1, 1, -2\}$ $A \cap B = \{-1, 1\}$
11	

12	$\sqrt{2 + \sqrt{2 + 2 \cos 4x}} = \sqrt{2 + \sqrt{2 + 2(2 \cos^2 2x - 1)}}$ <p>{since, <math>\cos 2x = 2 \cos^2 x - 1 \Rightarrow \cos 4x = 2 \cos^2 2x - 1</math>}</p> $= \sqrt{2 + \sqrt{2 + 4 \cos^2 2x - 2}}$ $= \sqrt{2 + \sqrt{4 \cos^2 2x}}$ $= \sqrt{2 + 2 \cos 2x}$ $= \sqrt{2 + 2(2 \cos^2 x - 1)}$ <p>{since, <math>\cos 2x = 2 \cos^2 x - 1</math>}</p> $= \sqrt{2 + 4 \cos^2 x - 2}$ $= \sqrt{4 \cos^2 x}$ $= 2 \cos x$ $= \text{RHS}$
13	$\text{LHS} = \frac{\sin(A-B)}{\sin(A+B)} = \frac{\sin A \cos B - \cos A \sin B}{\sin A \cos B + \cos A \sin B}$ $= \frac{\tan A - \tan B}{\tan A + \tan B} = \frac{x \tan B - \tan B}{x \tan B + \tan B}$ $= \frac{x-1}{x+1} = \text{RHS}$
14	<p>(i) <math>\{(-1, -1, -1), (-1, -1, 1), (-1, 1, -1), (1, -1, -1), (-1, 1, 1), (1, 1, -1), (1, -1, 1), (1, 1, 1)\}</math></p> <p>(iii) <math>D_f = [-5, 5]</math>    <math>R_f = [0, 5]</math></p>
15	<p><math>U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25\}</math></p> <p><math>A = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15\}</math></p> <p><math>B = \{11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25\}</math></p> <p>(i) Find <math>B - A</math>    - <b><math>\{16, 17, 18, 19, 20, 21, 22, 23, 24, 25\}</math></b></p> <p>(ii) Find <math>A \cup B</math>    - <math>U</math></p> <p>    - Find <math>(A - B)'</math>    - <math>B</math></p> <p>    - OR    -</p> <p>    Find <math>A' \cap B'</math>    - <math>\emptyset</math></p>